

Course and Examination Fact Sheet: Spring Semester 2024

6,252: Stochastic Methods in Finance

ECTS credits: 3

Overview examination/s

(binding regulations see below) decentral - Oral examination and technical discussions, Analog, Individual work individual grade (100%) Examination time: Term time

Attached courses

Timetable -- Language -- Lecturer 6,252,1.00 Stochastic Methods in Finance -- English -- Mahmoud Ola

Course information

Course prerequisites

Some previous exposure to probability and statistics will help in the learning process. The Bachelor level course Mathematics for Economists is useful, and in general a good level of mathematical interest and sophistication is required. The course is nevertheless fully self contained.

Learning objectives

The material of this course represents a first step that needs to be taken by any student interested in quantitative finance. This course is a good educational block for future practitioners in the financial industry as well as for those students that want to continue their studies in the applications of stochastic methods in finance and in financial econometrics. Upon completion of the course, the students will be familiar with the fundamentals of probability theory and stochastic calculus, no-arbitrage pricing techniques, and elementary portfolio optimization techniques.

Course content

The course introduces the fundamental stochastic tools for derivative asset pricing and portfolio theory. The ability to price and hedge derivative products and to properly manage asset portfolios is of paramount importance in the financial industry. The existing techniques to carry this out require a good command of the concepts in stochastic calculus that will be presented in this course. The two main mathematical methods used in this course are probability theory and stochastic calculus. These tools allow for a mathematically rigorous formulation of the hypotheses underlying the no-arbitrage approach to asset pricing and that yield explicit quantitative results that can be easily used in practice.

Course structure and indications of the learning and teaching design

- 1. Probability Theory:
- Introduction
- Distribution functions
- Normal distribution
- Multivariate normal distribution
- Lognormal distribution
- Binomial distribution
- 2. Pricing and No-arbitrage:
- Binomial model
- Fundamental asset pricing theorem
- 3. Ito's lemma and Stochastic Integrals:



- Random walk and Brownian motion
- Ito processes and Ito's lemma
- Derivative pricing
- Partial differential equations
- Stochastic differential equations
- 4. Risk Neutral Valuation:
- Discrete model
- Lognormal model
- Extensions
- 5. Markowitz Portfolio Theory:
- Markowitz approach
- Asset liability approach
- Shortfall constraint
- 6. Arbitrage Pricing Theory Model
- Discussion of the model
- Mathematical properties of the model
- 7. Portfolio Theory in Continuous Time
- Definition
- Extensions

Course literature

Course slides posted online.

Lamberton, D. and Lapeyre, B. "Introduction to stochastic calculus applied to finance". Chapman and Hall/CRC, 2008.

Neftci, S. N. "An Introduction to the Mathematics of Financial Derivatives". Academic Press, 2000.

Watsham, T. J. and Parramore, K. "Quantitative Methods in Finance". International. Thomson Business Press, 1997.

Additional course information

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Examination information

Examination sub part/s

1. Examination sub part (1/1)

Examination modalities

Examination type Oral examination and technical discussions

Responsible for organisation decentral

Examination form Oral examination

Examination mode Analog
Time of examination Term time
Examination execution Asynchronous
Examination location On Campus



Grading type Individual work individual grade

Weighting 100% Duration --

Examination languages Question language: English Answer language: English

Remark

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Examination-aid rule

Closed Book

The use of aids is prohibited as a matter of principle, with the exception of pocket calculator models of the Texas Instruments TI-30 series and, in case of non-language exams, bilingual dictionaries without any handwritten notes. Any other aids that are admissible must be explicitly listed by faculty members in the paragraph entitled "Supplementary aids" of the course and examination fact sheet; this list is exhaustive.

Procuring any aids, as well as ensuring their working order, is the exclusive responsibility of students.

Supplementary aids

No supplementary aid

Examination content

Contents presented in the lectures and reading assignments.

These include:

1. Probability Theory: - Introduction - Distribution functions - Normal distribution - Multivariate normal distribution - Lognormal distribution - Binomial distribution 2. Pricing and No-arbitrage: - Binomial model - Fundamental asset pricing theorem 3. Ito's lemma and Stochastic Integrals: - Random walk and Brownian motion - Ito processes and Ito's lemma - Derivative pricing - Partial differential equations - Stochastic differential equations 4. Risk Neutral Valuation: - Discrete model - Lognormal model - Extensions 5. Markowitz Portfolio Theory: - Markowitz approach - Asset liability approach - Shortfall constraint 6. Arbitrage Pricing Theory Model - Discussion of the model - Mathematical properties of the model 7. Portfolio Theory in Continuous Time - Definition - Extensions

Examination relevant literature

Lecture slides and reading assignments. All material will be uploaded on Canvas before the end of the term.



Please note

Please note that only this fact sheet and the examination schedule published at the time of bidding are binding and takes precedence over other information, such as information on StudyNet (Canvas), on lecturers' websites and information in lectures etc.

Any references and links to third-party content within the fact sheet are only of a supplementary, informative nature and lie outside the area of responsibility of the University of St.Gallen.

Documents and materials are only relevant for central examinations if they are available by the end of the lecture period (CW21) at the latest. In the case of centrally organised mid-term examinations, the documents and materials up to CW 13 are relevant for testing.

Binding nature of the fact sheets:

- Course information as well as examination date (organised centrally/decentrally) and form of examination: from bidding start in CW 04 (Thursday, 25 January 2024);
- Examination information (supplementary aids, examination contents, examination literature) for decentralised examinations: in CW 12 (Monday, 18 March 2024);
- Examination information (supplementary aids, examination contents, examination literature) for centrally organised mid-term examinations: in CW 13 (Monday, 25 March 2024);
- Examination information (regulations on aids, examination contents, examination literature) for centrally organised examinations: Starting with de-registration period in CW 15 (Monday, 08 April 2024).